Interpretation and Implementation of BCBS 457 - SBM Commodity

Atoti FRTB

5.1

Table of Contents

Commodity

This section describes how the SBM Commodity Risk Class is implemented and how the BCBS 457 specification is interpreted.

Also covered here is the specialization of the data, calculations, and configuration for the Commodity risk-class, including:

- The data model, which describes the data used for the calculations and how it is structured, and how the data model is represented in the:
    - input files
    - datastore
    - cube
- The calculations, both in the ETL and at query time
- The parameters used in the query time calculations
- How the Solution is configured for Commodity

Data Model (Core)

This section describes the data used for the Commodity calculations, including how the data is structured.

For Commodities, the Commodity (Underlying) refers to the "distinct commodity" [MAR21.83](1) and [MAR21.84].

The Risk Factor is used to identify sensitivities. However, it is not used directly in the calculations, instead the Commodity, Location, and tenor fields are used (as appropriate for the risk-measure). This means that multiple Risk Factor Names may be used for the same risk-factor.

Sensitivities

Field	Key	Risk Measure	Description
As-of Date	Y	All	Timestamp (at close of business) for the data (T-1)
Trade ID	Y	All	A unique identifier for the trade (or position)
Risk Factor Name	Y	All	A unique identifier for the risk-factor
Risk Class	Y	All	"Commodity"
Risk Measure	Y	All	"Delta", "Vega", or "Curvature"
Sensitivity Tenor	Y	Delta	The time to maturity of the traded instrument
Option Maturity	Y	Vega	The maturity of the option
Sensitivity		Delta & Vega	The sensitivity value s_k
Shock Up/Down		Curvature	The up and down shocked prices.

Field	Key	Risk Measure	Description
Sensitivity Currency		All	Currency in which the sensitivity or shocked price is expressed.
Risk Weight		Curvature	Risk weight used for the shocked prices
PV Applied		Curvature	Has the PV been subtracted from the shocked prices?
Optionality		Delta	Should the Delta sensitivity be included in the Curvature Calculation?
Interpolated Sensitivities		Delta & Vega	Sensitivities interpolated to the prescribed vertices

Risk Factor [MAR10.9]

The Risk Factor is used to identify sensitivities. However, it is not used directly in the calculations, instead the Commodity, Location, and tenor fields are used (as appropriate for the risk-measure). This means that multiple Risk Factor Names may be used for the same risk-factor.

The Commodity (Underlying) refers to the "distinct commodity" [MAR21.83](1) and [MAR21.84].

Field	Key	Risk Measure	Description
As-of Date	Y	All	Timestamp (at close of business) for the data (T-1)
Risk Factor Name	Y	All	A name for the risk-factor
Risk Class	Y	All	"Commodity"
Risk Measure	Y	All	"Delta", "Vega", or "Curvature"
Sensitivity Tenor	Y	Delta	The time to maturity of the traded instrument (Delta)
Option Maturity	Y	Vega	The maturity of the option (Vega)
Commodity (Underlying)		All	The distinct commodity
Location		All	Delivery location of the commodity

For Vega and Curvature, the risk-factor is the same as the underlying.

Commodity

The Commodity (Underlying) refers to the commodity [MAR21.13](1).

Field	Key	Description

Field	Key	Description
As-of Date	y	Timestamp (at close of business) for the data (T-1)
Commodity (Underlying)	Y	Name of the commodity
Risk Class	Y	"Commodity"
Bucket		1-11

Calculations

This section describes ETL from the reference implementation and the transformations / calculations applied to the sensitivities in the post-processors after they have been aggregated.

First, the ETL (Extract, Transform, Load) layer will apply some transformations as the data is loaded from the input files into the datastore.

Once the data is loaded into the datastore, it is available in the cube. The sensitivities in the cube may be partially aggregated upon commit to the datastore for BITMAP and LEAF aggregate providers. The remainder of the sensitivity aggregation is performed by Atoti Server at query time.

Then, also at query time, the post-processors calculate the capital charge from the aggregated sensitivities.

ETL (Reference Implementation)

The ETL (Extract, Transform, Load) layer provided with Atoti FRTB, using the default file format, will perform the following transformations when data is loaded from the input files into the datastore.

Risk Factor Name

If the risk-factor name is not included in the input file (using the default file format), a name is generated as follows:

- Delta: Commodity + Location
- Vega: Commodity
- Curvature: Commodity

Normalization

In the default file format, each row of the sensitivities' files contains the sensitivity as well as a description of the risk factor. The data normalization splits this information across two stores in the datastore, as described in the data model.

Vectorization

For efficiency, Delta and Vega sensitivities are stored in vectors. The entries of the vectors represent the tenors/maturities of the risk factors.

In the default file format, we allow sensitivities to be provided as either single values or as vectors. During the ETL, sensitivities are grouped together into vectors.

Interpolation

For compatibility with risk engines, Delta and Vega sensitivities may be loaded for any tenor/maturity. During the ETL, these sensitivities are interpolated to match the tenors/maturities in the specification.

Query Time (Core)

For the Commodity risk class, there are three main chains of post-processor calculations: Delta, Vega, and Curvature.

Delta and Vega

The calculation steps for Delta and Vega are the same:

1. The calculations start by applying currency conversion to the aggregated raw sensitivities from the cube to get the Sensitivities.
2. The risk-weights are applied to get the Weighted Sensitivities (per risk-factor).
3. The (rho) correlations are then used to calculate the Risk Position (per bucket).
4. The Risk Positions are combined across all buckets to calculate the Risk Charge.

In the bookmarks folder "ActiveViam FRTB" -> "Basel Framework" -> "SBM", the bookmarks "Commodity Delta" and "Commodity Vega" contain tabs that walk through these calculation steps and include the measures mentioned here.

Curvature

For Curvature, the calculation steps are:

1. Start with vectors of shocked prices indexed by risk-weight (per risk-factor).
2. The risk-weight then determines which Shock Up/Down Prices we want, subtracting the trade PV if necessary.
3. The delta sensitivities are filtered sensitivities from the Delta calculations, and aggregated per Curvature risk-factor.
4. These are then combined to calculate the CVR Up/Down (per risk-factor).
5. The Risk Position Up/Down are calculated per bucket.
6. The greater of the up and down risk-positions is identified by the Risk Position Scenario, and used for the Risk Position (per bucket).
7. The Risk Positions are combined across all buckets to calculate the Risk Charge.

The bookmark "ActiveViam FRTB" -> "Basel Framework" -> "SBM" -> "Commodity Curvature" contains tabs that walk through these calculation steps and includes the measures mentioned here.

Delta/Vega Sensitivities

The Delta/Vega Sensitivities measures are the s_k in [MAR21.4](1) and (2).

For each Sensitivity Currency, the Interpolated Sensitivities are converted to the reference currency

using the IFxRates API (supplied by the reference implementation). After this currency conversion, the values are aggregated for each Risk Factor.

Delta Sensitivities Long/Short

The Delta Sensitivities Long/Short measures are the Positive or Negative Delta Sensitivities.

The Positive or Negative determination is made at the Commodity, Location and Tenor levels.

Curvature Scenario Up/Down PV.CCY

The Scenario Up/Down PV.CCY measures are vectors of shocked prices indexed by risk weight.

For each Sensitivity Currency, the Shock Up/Down prices are converted to the reference currency using the IFxRates API. After this currency conversion, the values are aggregated for each Risk Factor.

Delta/Vega/Curvature Risk Weight

The Delta/Vega/Curvature Risk Weight measures are RW_k in [MAR21.4](3) and $RW_k^{(Curvature)}$ in [MAR21.5](2)(e).

For Delta and Curvature, following [MAR21.82], the values are looked up based on the configuration for the Risk Factor's Bucket.

For Vega, following [MAR21.92], the value is looked up based on the configuration for the Risk Class (and its liquidity horizon).

Delta/Vega Weighted Sensitivities

The Delta/Vega Weighted Sensitivities measures are WS_k in [MAR21.4](3).

For each Risk Factor k, the Delta/Vega Sensitivities measures are multiplied by the Delta/Vega Risk Weight.

Curvature Delta Sensitivities

The Curvature Delta Sensitivities measure is s_{ik} in [MAR21.5](2)(f).

For each Curvature Risk Factor k, it is all the Delta Sensitivities with the same Commodity as the risk factor, filtered by Optionality.

Curvature Shock Up/Down Prices

The Curvature shock-up/down prices measures are $V_i\left(x_k^{RW^{(Curvature)}\pm}\right) - V_i(x_k)$ in [MAR21.5](2).

Using linear interpolation, the shocked prices corresponding to the Curvature Risk Weight are determined from the Curvature Scenario UP/Down.CCY vectors. And, if PV Applied is not true/yes, the trade PV is subtracted.

Curvature CVR Up/Down

The Curvature CVR Up/Down measures are $CVR_k^{\pm}$ in [MAR21.5](2).

The Curvature Delta Sensitivities are multiplied by the Curvature Risk Weight and subtracted

from/added to the Curvature Shocked Up/Down Prices (respectively).

Delta/Vega Risk Position Double Sums

The Delta/Vega Risk Position Double Sums measures are the $\sum_k \sum_l WS_k \cdot WS_l$ intermediate values that were requested for the 2017 and 2018 QIS exercises.

Within each Bucket, each pair of Risk Factors, is categorised according to:

- Delta

    - Same or different Commodity
    - Same or different Tenor
    - Same or different Location

- Vega

    - Same or different Commodity
    - Combinations of Option Maturities

Within each category, the pairs of Delta/Vega Weighted Sensitivities are multiplied together and summed.

Implementation Note: This calculation has been optimized so that it is performed with $O(N)$ (linear) time complexity, where N is the number of Risk Factors.

Delta/Vega Risk Position Correlations

The Delta/Vega Risk Position Correlation measures are ρ_{kl} in [MAR21.4](4).

Within each Bucket, and for each category of Risk Factor pairs (see Delta/Vega Risk Position Double Sums) the values are looked up from the configuration for [MAR21.83] and [MAR21.94].

Note: The $\rho_{kl}^{(Delta)}$ in [MAR21.94] is equivalent to $\rho_{kl}^{(cty)}$ in [MAR21.83] as the Vega Risk Factors are not differentiated by the Delta Sensitivity Tenor or Location.

Delta Vega Risk Position

The Delta/Vega Risk Position measures are K_b in [MAR21.4](4).

For each Bucket, the Delta/Vega Risk Position is calculated from the Delta/Vega Weighted Sensitivities and Delta/Vega Risk Position Correlations using the formula in [MAR21.4](4).

Implementation Note: This calculation has been optimized so that it is performed with $O(N)$ (linear) time complexity, where N is the number of Risk Factors.

Curvature Risk Position Up/Down

The Curvature Risk Position Up/Down measures are $K_b^{\pm}$ in [MAR21.5](3).

Within each Bucket, the Curvature CVR Up/Down values are combined using the formula in [MAR21.5](3).

Implementation Note: This calculation has been optimized so that it is performed with $O(N)$ (linear) time complexity, where N is the number of Risk Factors.

Curvature Risk Position Scenario

Within each Bucket, the Curvature Risk Position Scenario measure identifies which of the Curvature Risk Position Up and Curvature Risk Position Down values is the greater.

Curvature Risk Position

The Curvature Risk Position measure is K_b in [MAR21.5](3).

Within each Bucket, it is the greater of the Curvature Risk Position Up and Curvature Risk Position Down values.

Delta/Vega Risk Charge

The Delta/Vega Risk Charge measures are Delta and Vega in [MAR21.4](5).

They are calculated by combining the Delta/Vega Risk Positions (and aggregated Delta/Vega Weighted Sensitivities) over all Buckets according to [MAR21.4](5).

Curvature Risk Charge

The Curvature Risk Charge measure is $\mathrm{Curvature\ risk}$ in [MAR21.5](4).

It is calculated by combining the Curvature Risk Positions (and aggregated CVR Up or CVR Down values) over all Buckets according to [MAR21.5](4).

Input Files (Reference Implementation)

This section describes how the input files containing the sensitivities and mappings are used for the Commodity risk class

The sensitivities are loaded from the Delta, Vega, Curvature, or CRIF sensitivity files.

The mapping of Underlying to Bucket is loaded from the Commodity Buckets file into the CommodityBuckets store.

SBM_Delta_Sensitivities*.csv

The Delta Sensitivity Data is loaded from the Delta files.

The following table lists the fields in the file format that is used for the Commodity risk-class. See the Delta file format documentation for details on the file format. See Data Model (Core) for a description of the data model.

Data Model Field	File Column	Notes
As-Of Date	AsOfDate	
Trade ID	TradeID	
Sensitivity Currency	DeltaCcy	

Data Model Field	File Column	Notes
Sensitivities	DeltaSensitivities	May be single value or vector, with the same number of entries as Tenors.
Risk Class	RiskClass	"Commodity"
Sensitivity Tenor	SensitivityDates	May be single value, vector, or empty. If empty, treated as the prescribed tenors: 0;0.25;0.5;1;2;3;5;10;15;20;30.
Risk Factor Name	RiskFactor	(Optional) If not present, generated during ETL.
Commodity	Underlying	
Bucket	Bucket	1-11
Location	CommodityLocation	
Optionality	Optionality	Should this sensitivity be included in the Curvature calculations ('Y') or not ('N')?

SBM_Vega_Sensitivities*.csv

The Vega Sensitivity Data is loaded from the Vega files.

The following table lists the fields in the file format that is used for the Commodity risk-class. See the Vega file format documentation for details on the file format. See Data Model (Core) for a description of the data model.

Data Model Field	File Column	Notes
As-Of Date	AsOfDate	
Trade ID	TradeID	
Risk Class	RiskClass	"Commodity"
Option Maturity	OptionMaturity	May be single value, vector, or empty. If empty, treated as the prescribed maturities: 0.5;1;3;5;10.
Sensitivities	VegaSensitivities	May be single value or vector, with the same number of entries as maturities.
Sensitivity Currency	VegaCcy	
Risk Factor Name	RiskFactor	(Optional) If not present, generated during ETL.

Data Model Field	File Column	Notes
Commodity	Underlying	
Bucket	Bucket	1-11

SBM_Curvature_Sensitivities*.csv

The Curvature Sensitivity Data is loaded from the Curvature files.

The following table lists the fields in the file format that are used for the Commodity risk-class. See the Curvature file format documentation for details on the file format. See Data Model (Core) for a description of the data model.

Data Model Field	File Column	Notes
As-Of Date	AsOfDate	
Trade ID	TradeID	
Risk Class	RiskClass	"Commodity"
Risk Factor Name	RiskFactor	(Optional) If not present, generated during ETL.
Shock Up	Shift_Up_PV	
Shock Down	Shift_Down_PV	
Sensitivity Currency	CurvatureCcy	
Risk Weight	RiskWeight	(Optional)
PV Applied	PV Applied	Has the Trade PV already been subtracted from the shocked PVs ('Y') or not ('N')?
Commodity	Underlying	
Bucket	Bucket	1-11

Datastore (Reference Implementation)

This section describes how the SA datastore schema is used for the Commodity risk class.

The schema starts with the SaSensitivities store, which is an index of all the facts in the SA Cube. The SaSensitivities store has references to the risk-factor descriptions and sensitivities.

Risk Factor Descriptions

The risk-factor description starts with the RiskFactorDescription store, which contains the description of risk-factor independent of the commodity, and a reference to the UnderlyingDescription store for a description of the commodity.

Sensitivities

The sensitivities stores contain the sensitivity values, they are referenced from the TradeBase store.

Risk Measure	Sensitivity Store
Delta	Delta
Vega	Vega
Curvature	Curvature

TradeBase

The SaSensitivities store is the base store in the SA Cube Schema. Each row in this table represents a fact in the SA Cube.

The following table lists the fields in the store that are used for the Commodity risk-class. See the SaSensitivities store documentation for details on the store. See Data Model (Core) for a description of the data model.

Data Model Field	Store Field	Notes
As-Of Date	AsOfDate	
Trade ID	TradeId	
Risk Factor Name	Risk Factor	
Risk Class	RiskClass	"Commodity"
Risk Measure	Risk Measure	"Delta", "Vega", or "Curvature"

RiskFactorDescription

The RiskFactorDescription store contains the description of risk-factor.

The following table lists the fields in the store that are used for the Commodity risk-class. See the RiskFactorDescription store documentation for details on the store.

Data Model Field	Store Field	Notes
As-Of Date	AsOfDate	
Risk Factor Name	Risk Factor	
Risk Class	RiskClass	"Commodity"

Data Model Field	Store Field	Notes
Risk Measure	Risk Measure	"Delta", "Vega", or "Curvature"
Commodity	Underlying	
Location	CommodityLocation	
Sensitivity Tenors	Maturity	for Vega only

UnderlyingDescription

The UnderlyingDescription store contains the description of the commodity.

The following table lists the fields in the store that are used for the Commodity risk-class. See the UnderlyingDescription store documentation for details on the store.

Data Model Field	Store Field	Notes
As-Of Date	AsOfDate	
Commodity	Underlying	
Risk Class	RiskClass	"Commodity"
Bucket	Bucket	

Delta

The SaSensitivities store contains the Delta sensitivities.

The following table lists the fields in the store that are used for the Commodity risk-class. See the SaSensitivities store documentation for details on the store.

Data Model Field	Store Field	Notes
As-Of Date	AsOfDate	
Trade ID	TradeId	
Risk Factor Name	Risk Factor	
Risk Class	RiskClass	"Commodity"
Risk Measure	Risk Measure	"Delta"
Sensitivity Currency	Ccy	
Sensitivities	DeltaSensitivities	
Optionality	Optionality	'Y' or 'N'

Vega

The SaSensitivities store contains the Vega sensitivities.

The following table lists the fields in the store that are used for the Commodity risk-class. See the SaSensitivities store documentation for details on the store.

Data Model Field	Store Field	Notes
As-Of Date	AsOfDate	
Trade ID	TradeId	
Risk Factor Name	Risk Factor	
Risk Class	RiskClass	"Commodity"
Risk Measure	Risk Measure	"Vega"
Sensitivity Currency	Ccy	
Sensitivities	VegaSensitivities	

Curvature

The SaSensitivities store contains the Curvature shocked prices.

The following table lists the fields in the store that are used for the Commodity risk-class. See the SaSensitivities store documentation for details on the store.

Data Model Field	Store Field	Notes
As-Of Date	AsOfDate	
Trade ID	TradeId	
Risk Factor Name	Risk Factor	
Risk Class	RiskClass	"Commodity"
Risk Measure	Risk Measure	"Curvature"
Shock Up	Shift_Up_PV	Vector-valued. Same size as Risk Weight
Shock Down	Shift_Down_PV	Vector-valued. Same size as Risk Weight
Risk Weight	RiskWeight	(optional) Vector-valued
PV Applied	PVApplied	'Y' or 'N'
Sensitivity Currency	Ccy	

CommodityBuckets

The CommodityBuckets store is used by the ETL to populate the Bucket.

See the CommodityBucket store documentation for details on the store.

Data Model Field	Store Field	Notes
Commodity	Underlying	
Bucket	Bucket	1-11

Cube Schema (Reference Implementation)

The following table lists the levels and hierarchies in the Cube schema that are used in the Commodity data model.

Data Model Field	Cube Level	Notes
As-Of Date	AsOfDate	Slicing Hierarchy
Trade ID	TradeId	
Risk Class	Risk Class	"Commodity"
Risk Measure	Risk Measure	"Delta", "Vega", "Curvature"
Bucket	Commodity Bucket	
Risk Factor Name	Risk Factor	
Sensitivity Tenor / Option Maturity	Vertex	Analysis Hierarchy
Commodity	Underlying	
Location	Commodity Location	
		Levels for the Delta Double Sums and Correlations
		Levels for the Vega Double Sums and Correlations

Configuration (Core)

This section describes how the calculations are configured for the Commodity risk class

Bucket Risk Weights

Maps Buckets to Risk Weights.

The file Commodity_BucketRiskWeights*.csv is loaded into the CommodityBucketRiskWeights store.

Data Model Field	File Column	Datastore Column	Notes
Bucket	Bucket	Bucket	1-11
RW_k in [MAR21.82]	Risk Weight	RiskWeight	
	Description	Description	Name of the bucket

Intra-Bucket Correlations

Maps Buckets to $\rho_{kl}^{(cty)}$ correlations.

The file Commodity_IntraBucketCorrelations*.csv is loaded into the CommodityIntraBucketCorrelations store.

Data Model Field	File Column	Datastore Column	Notes
Bucket	Bucket	Bucket	1-11
$\rho_{kl}^{(cty)}$ in [MAR21.83]	Correlation	Correlation	
	Description	Description	Name of the bucket

Vertices

The list of Commodity Delta Tenors and Vega Option Maturities.

The file Vertices*.csv is loaded into the Vertices store.

Data Model Field	File Column	Datastore Column	Notes
	Index	Index	0-11 (Delta) 0-4 (Vega)
Sensitivity Tenor / Option Maturity	Vertex	Vertex	Delta Tenors in [MAR21.13](1)(b) Vega Option Maturities in [MAR21.13](2)
Risk Class	Risk Class	RiskClass	"Commodity"
Risk Measure	Risk Measure	Risk Measure	"Delta" or "Vega"

Vega Liquidity Horizons

The file Vega_Liquidity_Horizons*.csv is loaded into the VegaRiskWeights store.

Data Model Field	File Column	Datastore Column	Notes
Risk Class	Risk Class	RiskClass	"Commodity"

Data Model Field	File Column	Datastore Column	Notes
$LH_{\text{risk class}}$ in [MAR21.92]	Vega LH	Liquidity Horizon	"120"

Miscellaneous Parameters

The file FRTBParameters*.csv is loaded into the FRTBParameters store.

Parameter	Parameter Name	Default Value
$\rho_{kl}^{(tenor)}$ in [MAR21.83](2)	sa.commodity.rho-tenor.correlation	0.99
$\rho_{kl}^{(basis)}$ in [MAR21.83](3)	sa.commodity.rho-basis.correlation	0.999
γ_{bc} in [MAR21.85](1)	sa.commodity.correlation	0.2
γ_{bc} in [MAR21.85](2)	sa.commodity.other-commodity.correlation	0
RW_σ in [MAR21.92]	sa.vega.rw	0.55
α in [MAR21.93](1)(a)	sa.vega.rho-option-maturity.alpha	0.01